

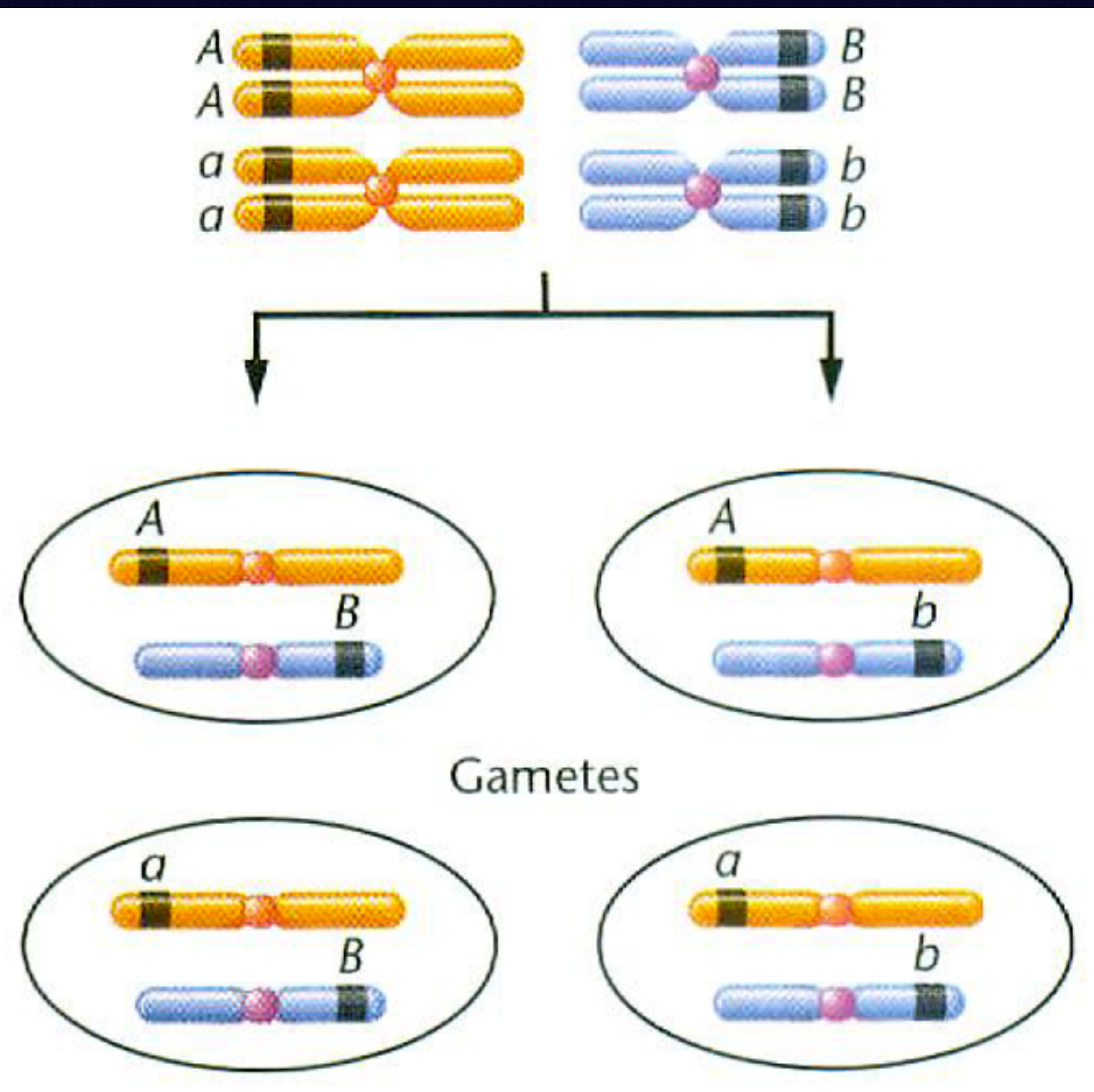
# Human linkage analysis

fundamental concepts



# Genes and chromosomes

Alleles of genes located on different chromosomes show independent assortment (Mendel's 2nd law)

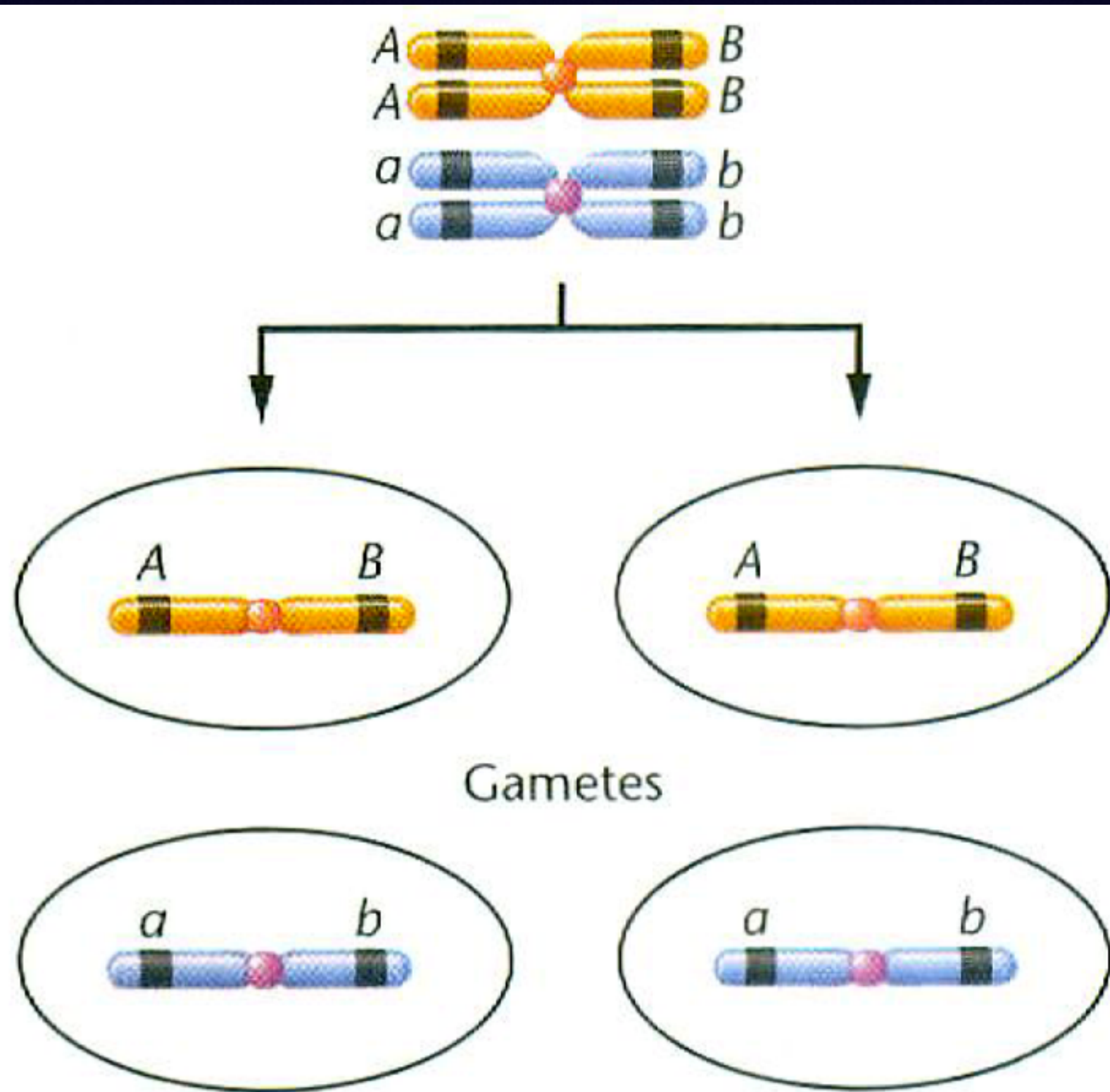


For 2 genes:  
4 gamete classes with equal number



# Linkage

Alleles of genes located on the same chromosome tend to segregate together - linkage

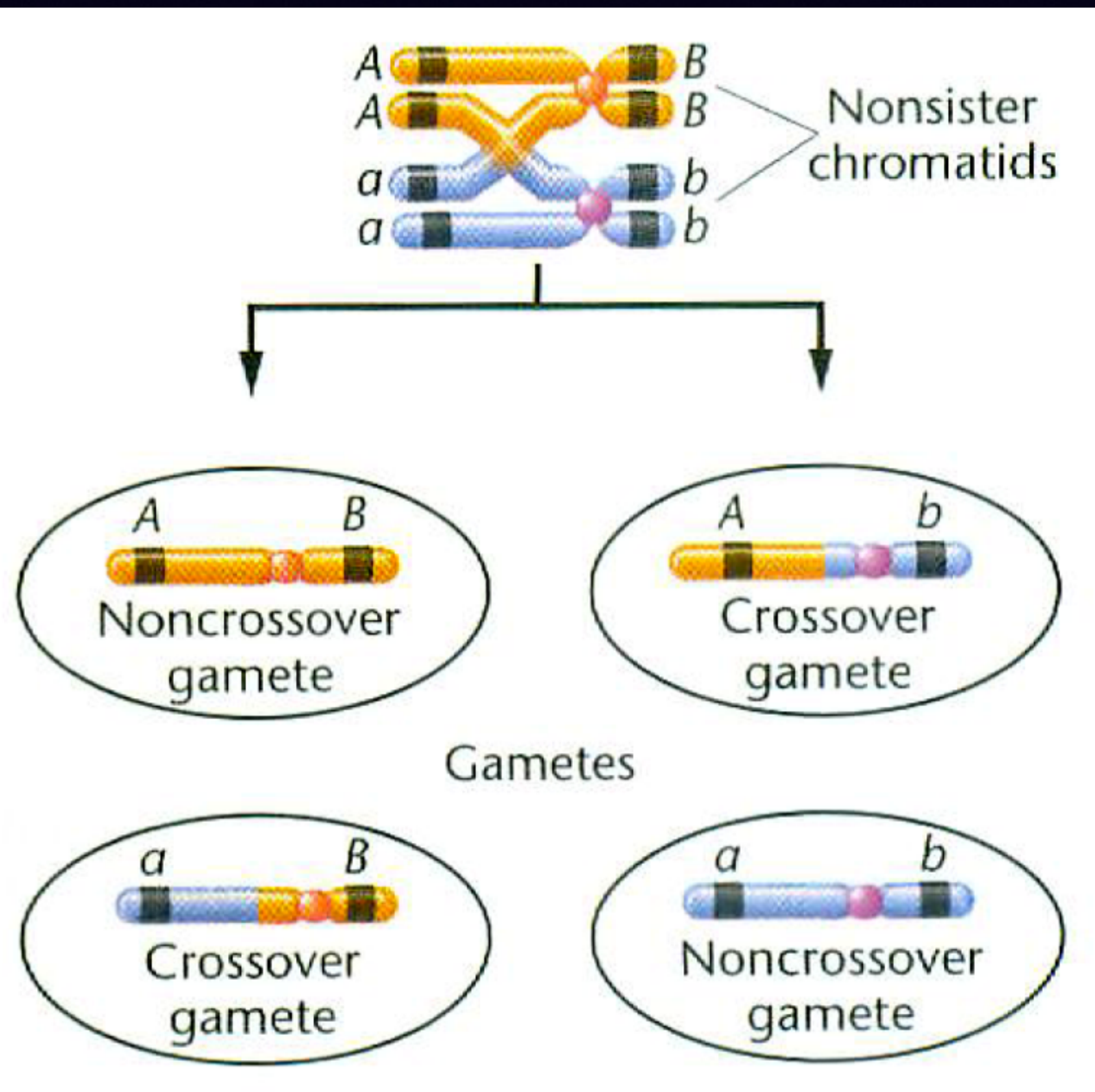


For 2 genes and complete linkage:  
2 parental genotype gamete classes



# Linkage

Crossing-over (non-sister chromatid exchange by meiotic recombination)

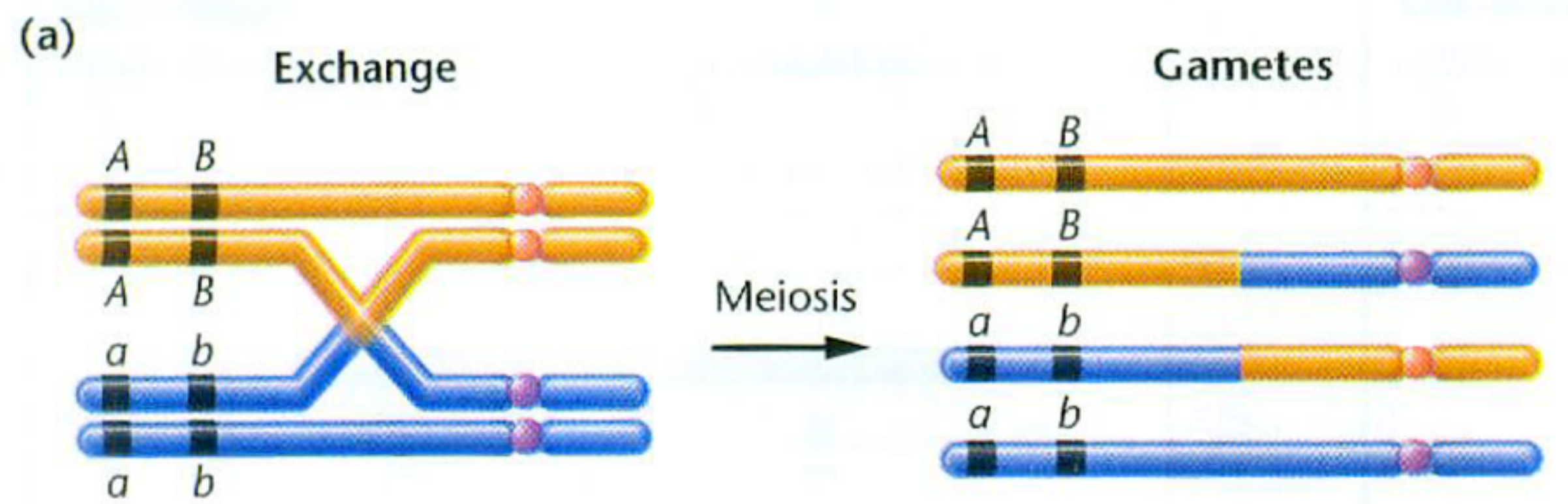


For 2 genes:  
2 parental (noncrossover) classes  
2 recombinant (crossover) classes  
Fewer recombinant than parental gametes

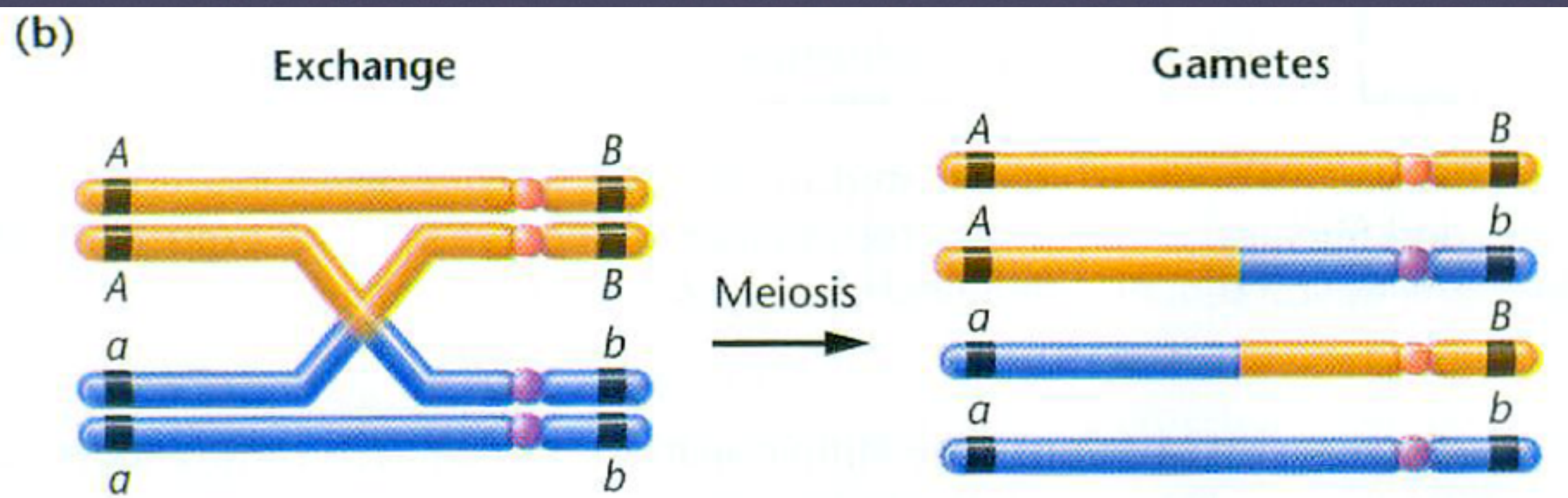


# Linkage mapping

To form recombinant gametes, a crossover has to occur **between** the gene loci



non-recombinant gametes form



recombinant gametes form



# Principles of linkage mapping

- The crossing-over probability between gene loci is proportional to the distance separating them on the chromosome
- The number of recombinant genotypes in the offspring measures the genetic distance
- In *Drosophila* the easiest way is to cross a double heterozygous female with a double recessive male
- How about human?



# Association vs. linkage

- Linkage - co-segregation of alleles of genes located on the same chromosome
  - involves gene loci, regardless of the allele
  - a simple biological mechanism (chromosomes, recombination)
  - studied in pedigrees or pairs of related individuals
  - used to study Mendelian traits - high heritability, alleles of single (or few) genes cause the phenotype



# Association vs. linkage

- Association - a correlation between gene alleles and traits in a population
  - always involves particular alleles
  - biological mechanism often complex or unknown - a statistical phenomenon, can be indirect
  - studied in a population of individuals, not from the same family
  - used to study multifactorial inheritance
  - can be related to linkage in a special case (linkage disequilibrium)



# Linkage disequilibrium

Allele of the gene *d* linked with the marker locus *A* mutated to the disease allele *D* - founder event



If the *A* to *d* distance is small, then most chromosomes that carry *D* also carry *A1*

Not vice versa (most chromosomes with *A1* need not carry *D*)!

Linkage disequilibrium) – nonrandom association of alleles in linked loci – founder effect. Decreases over time.



# Methods

- Linkage analysis - genetic mapping
  - parametric methods
  - nonparametric methods
- Association - correlation studies (statistical)



# Linkage in the human genome

- Human genes are usually located far from each other, with large intergenic regions
- Linkage between two genes with observable phenotypes is extremely rare
- Molecular markers (RFLP, VNTR, etc.) are used
  - human genome linkage maps, e.g. CEPH
  - finding a marker linked to a disease locus



# Linkage between a marker locus and a disease gene

- Association in a family (among related individuals)
- Usually no population-level association
- Independent of the population structure
- Linkage disequilibrium on the population level for very rare alleles



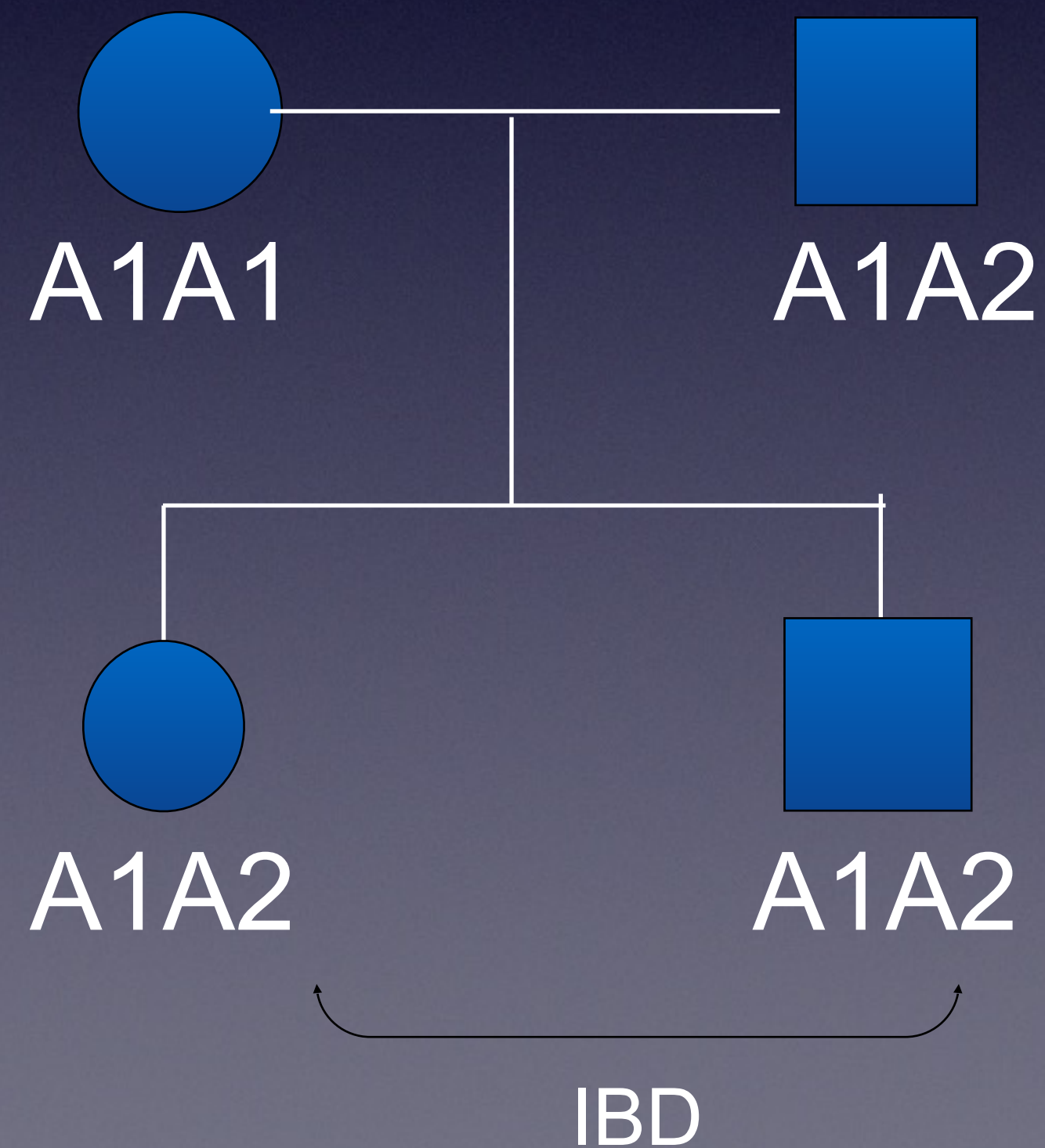
# Mapping methods

- Parametric (based on a model of inheritance): lod-score analysis
  - two-point
  - multipoint
- Nonparametric linkage analysis
  - correlation between alleles in related individuals
  - IBD (identity by descent) vs. IBS (identity by state)



# Nonparametric analysis

Two alleles are identical by descent (IBD) if they are copies of the same ancestral allele





# Nonparametric methods

- Correlation of the phenotype and the coincidence of a particular marker allele
  - Twin studies
  - Affected siblings method
  - Family studies (2-3 generations)
  - Affected siblings method: in pairs of affected siblings are the marker alleles (any) identical more often, then in the control population?



# Parametric methods

- In *Drosophila* the easiest way is to cross a double heterozygous female with a double recessive male
- How about human?



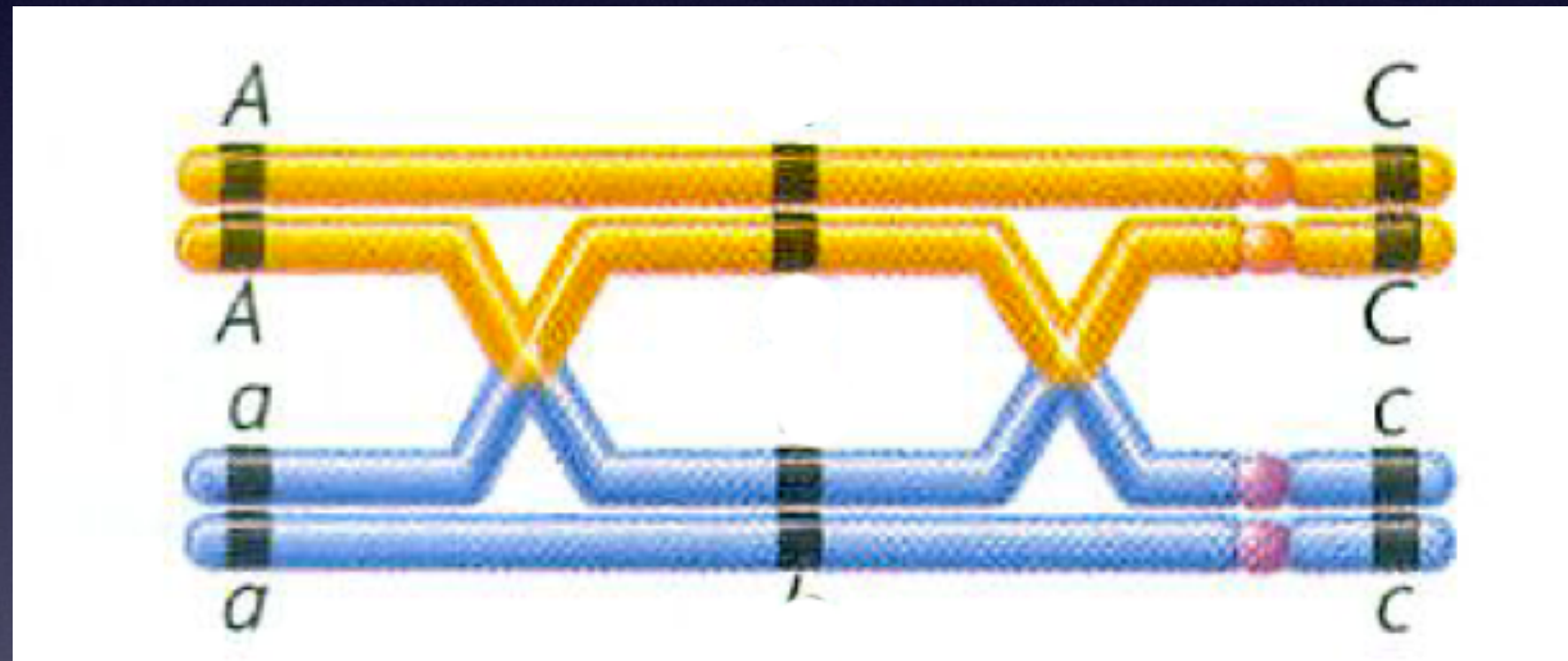
# Recombination frequency is a measure of genetic distance

- Recombination frequency  $\theta$  = probability of transmission of a recombinant gamete
- Loci on separate chromosomes segregate independently  
 $\Rightarrow \theta = 0.5$
- Tightly linked loci segregate together  
 $\Rightarrow \theta = 0$
- Therefore
  - $\theta < 0.5$  linkage
  - $\theta = 0.5$  no linkage



# Linkage mapping

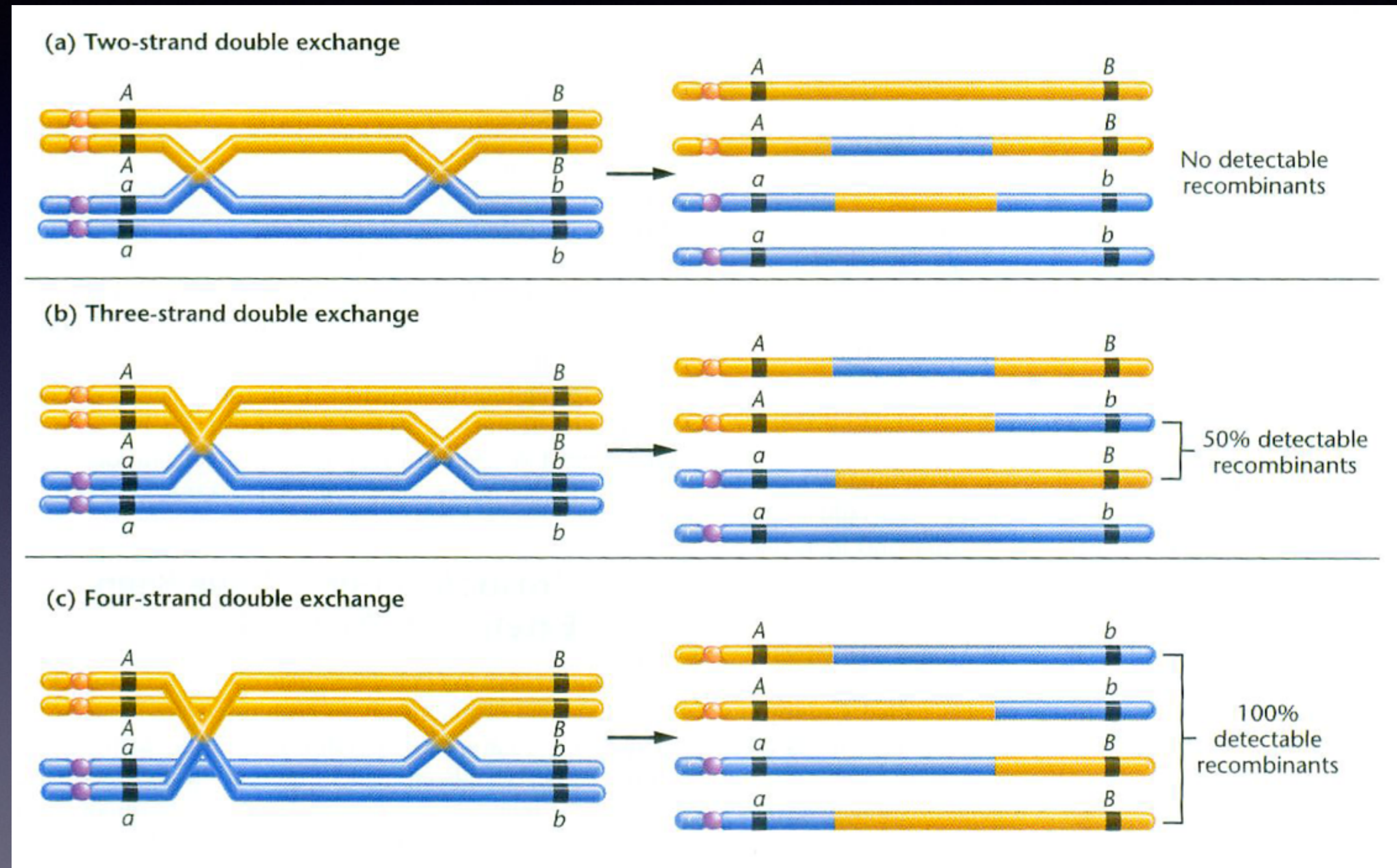
- Unit: cM (centimorgan) = 1% recombination frequency
- The correlation is not linear



- Double crossing-over – parental type gametes
- Interference – crossing-over in one region influences the probability of c-o in nearby regions



# Double c-o – a complex picture



On average 50% recombinants. Similarly for triple, etc.



# Mapping function

- Genetic distance as a function of observed recombinant frequency
- Haldane's function
  - multiple c-o, no interference
- Kosambi's function
  - multiple c-o, interference, commonly used
- For small  $\theta$ :  $d \approx \theta$

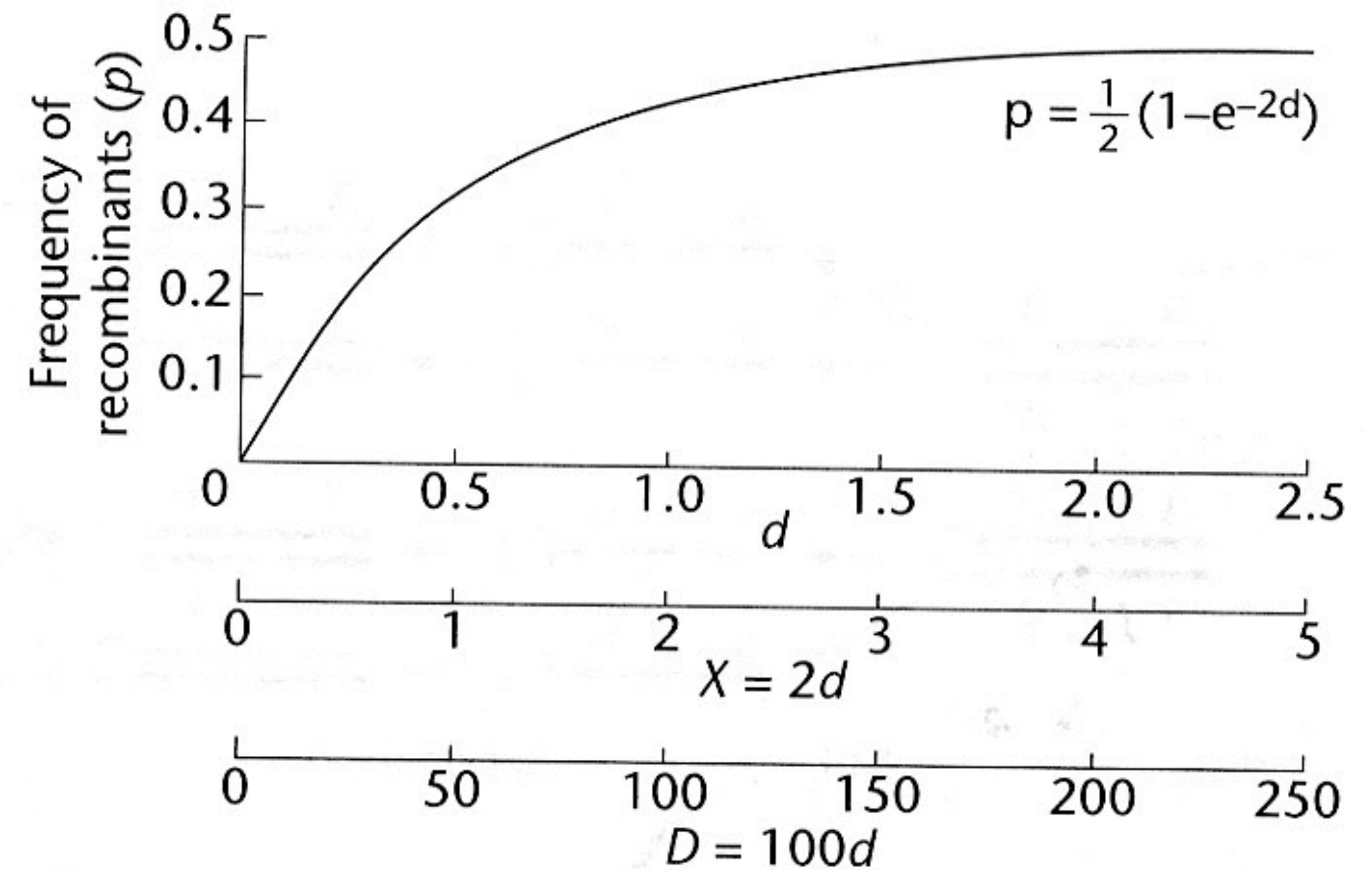
$$d = \frac{\ln(1 - 2\theta)}{2}$$

$$d = \frac{\ln\left(\frac{1 + 2\theta}{1 - 2\theta}\right)}{4}$$



# Mapping function

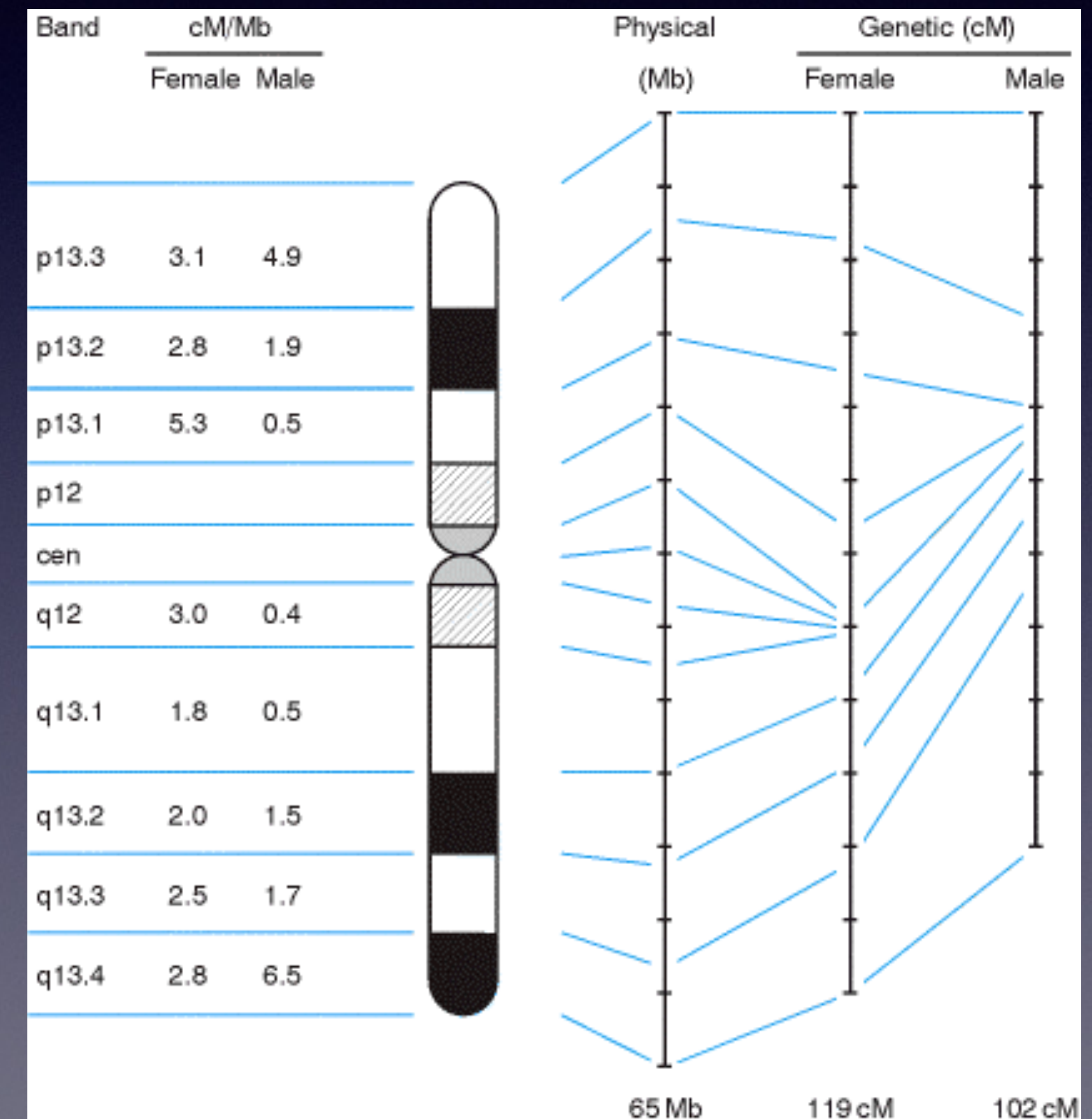
- Observed frequency of recombinants approaches 0.5 with increasing distance
- For unlinked genes 50% “recombinants”, like for genes far apart on the chromosome





# Sex and recombination frequency

- Total male genetic map = 2851cM (autosomal)
- Total female genetic map = 4296 cM (autosomal)
- For ~3000Mb of autosomal genome
  - 1 cM in males  $\approx$  1.05 Mb
  - 1 cM in females  $\approx$  0.7 Mb
  - average 1 cM  $\approx$  0.88 Mb
- the male/female ratio varies across genome





# Likelihood

- Likelihood: the probability of obtaining the observed data under assumptions of a tested model



# Likelihood in pedigree analysis

- In a fully informative pedigree
  - data:  $R$ =number of recombinants;  $NR$ =number of parental genotypes
  - the parameter: recombination frequency (probability)  $\theta$
- Null hypothesis – no linkage ( $\theta=0.5$ )
- Likelihood ratio  $L(\theta)/L(\theta=0.5)$
- lod score ( $Z$ ) = logarithm of odds – decimal logarithm of the likelihood ratio



# Simple lod score calculations

For each pedigree (i), the lod score is:

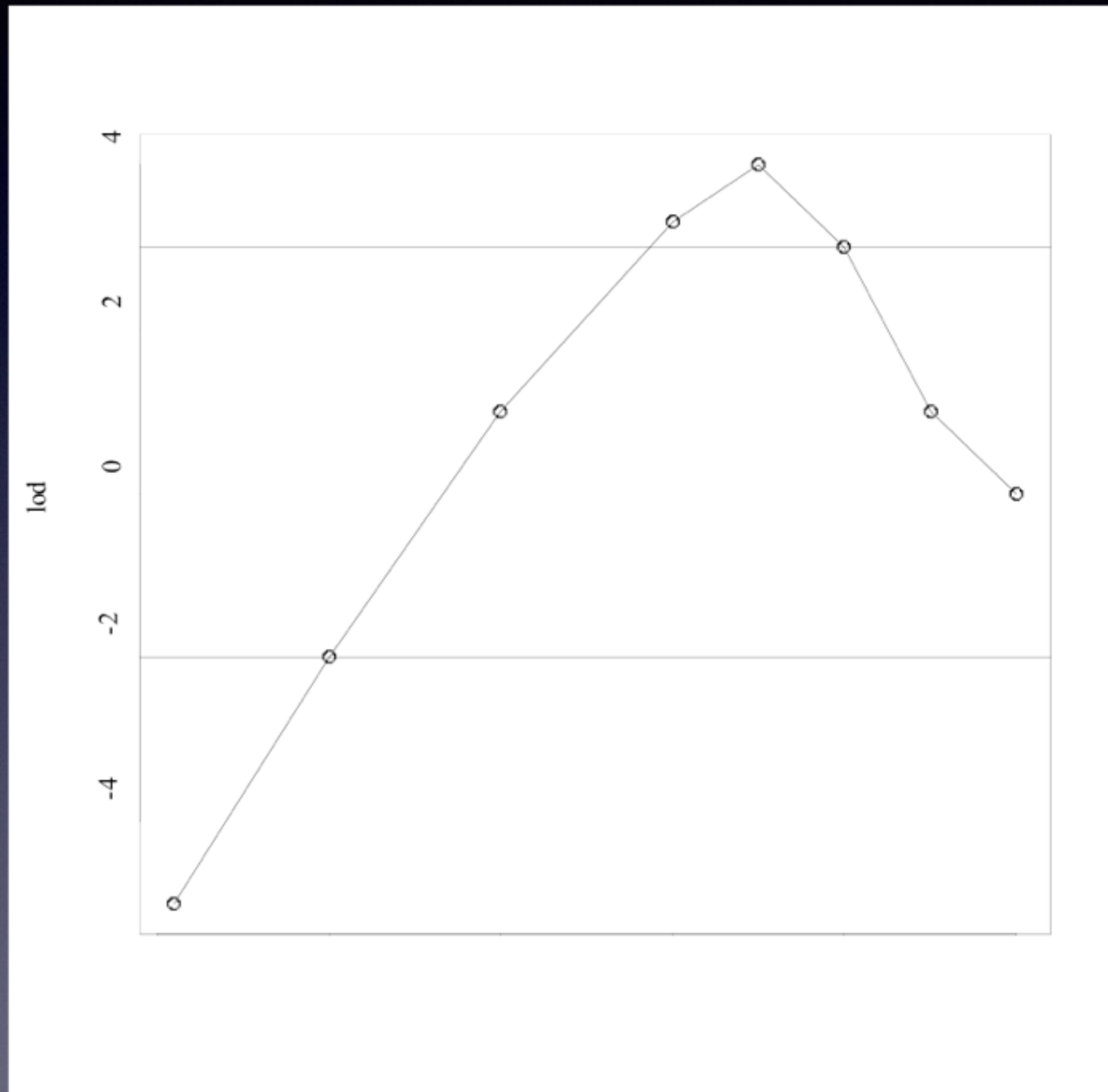
$$Z_i(\theta) = \log_{10} \frac{L(\text{pedigree} / \theta)}{L(\text{pedigree} / \theta = 0.5)}$$

For each  $\theta$ , lod-score is summed across pedigrees (F):

$$Z(\theta) = \sum_{i=1}^F Z_i(\theta)$$



# Two-point linkage analysis



significance  
( $Z > 3$ ,  $Z > 2$  for X-linked)

excluded

**Table**

$\theta =$	0.01,	0.10,	0.20,	0.30,	0.35,	0.40,	0.45,	0.50
lod=	-5.0,	-2.0,	1.0,	3.3,	4.0,	3.0,	1.0,	0.0

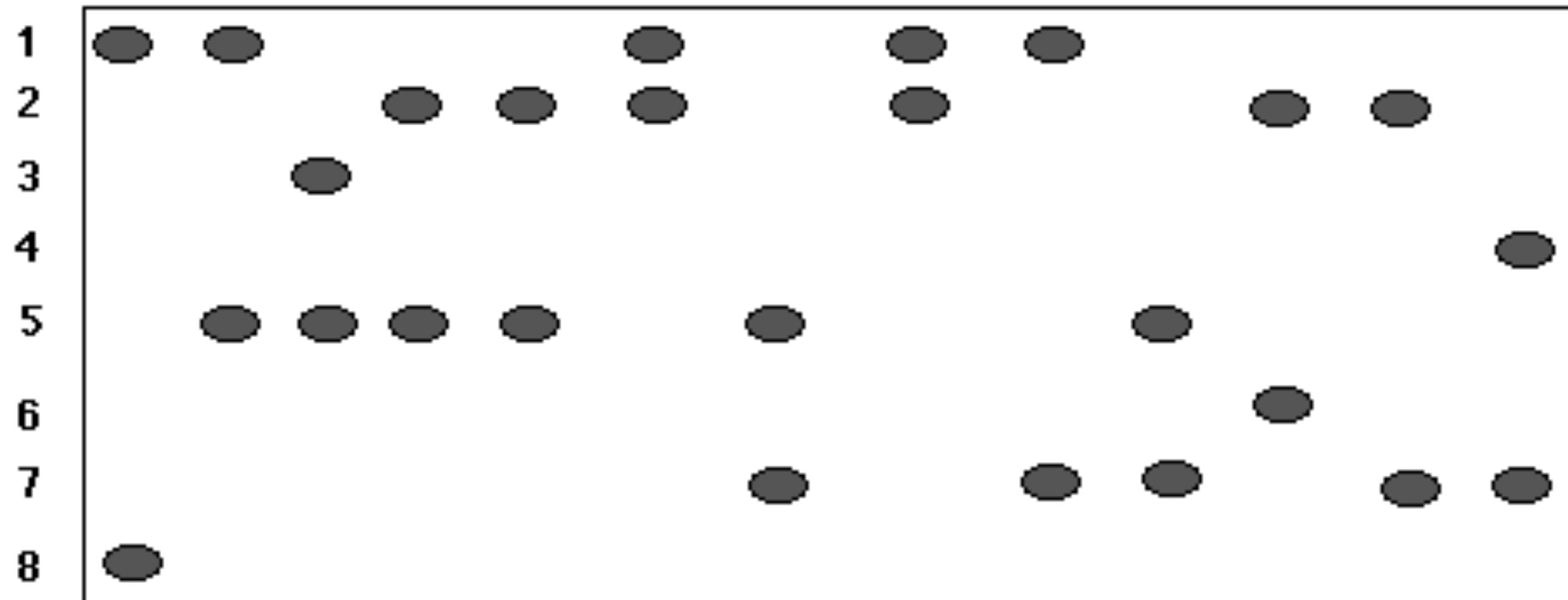
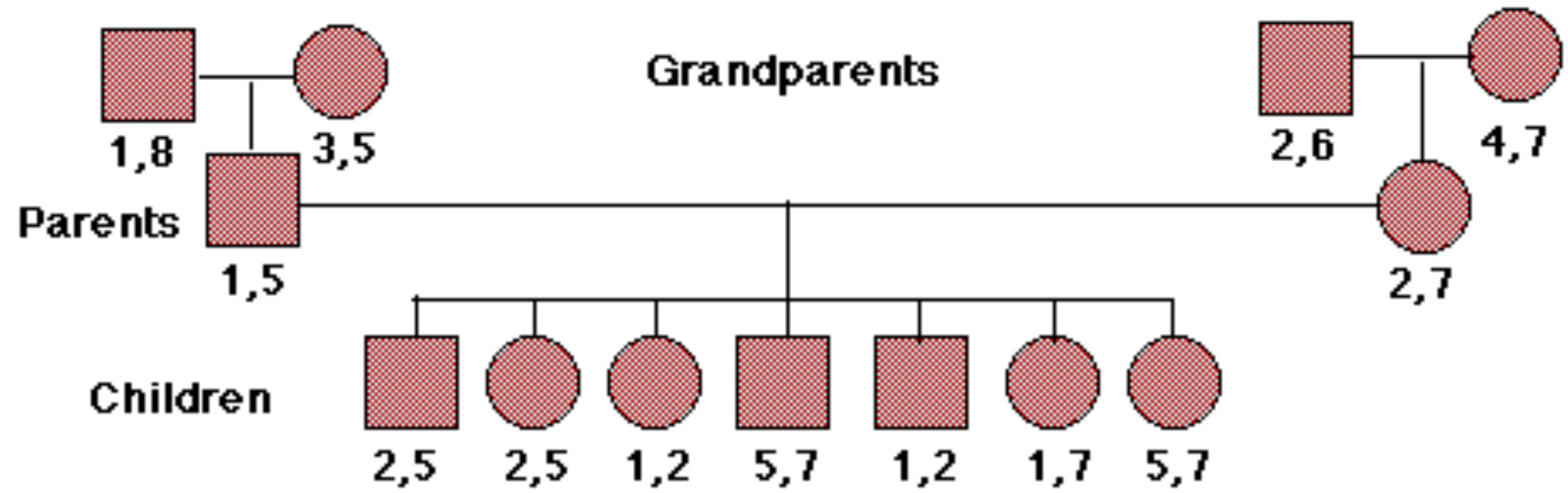


# Markers in human linkage analysis

- Linkage of two genes with an observable phenotype - extremely rare
  - exception – NPS – Nail Patella Syndrome and ABO blood groups
  - MHC loci
- Molecular markers
  - PCR, RFLP



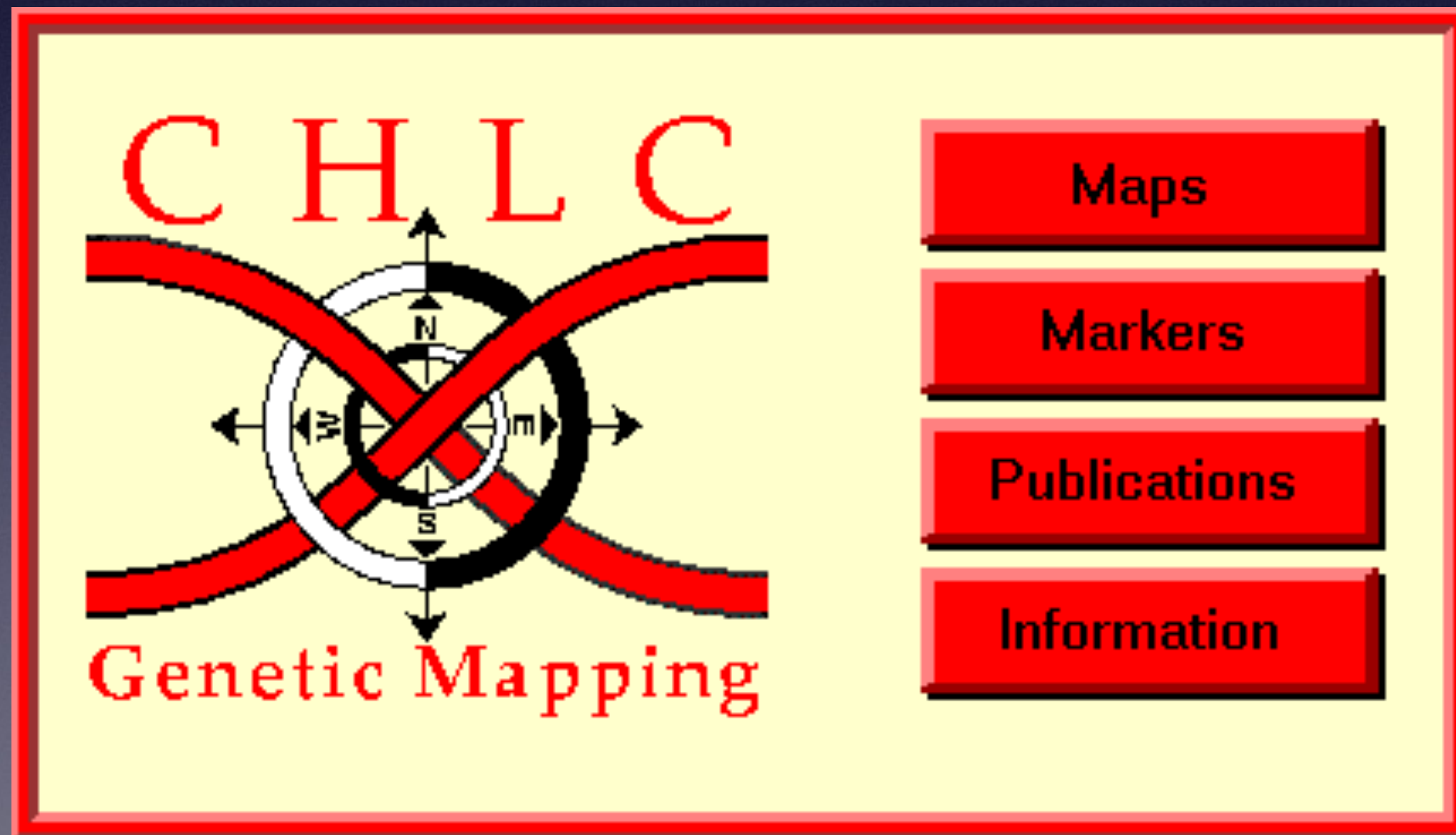
# Markers





# Finding a gene

- I stage – general (markers spaced 8-20 cM) – define the chromosome, is it a single locus, etc.
- II stage – fine-mapping (markers spaced 1-4 cM)





# Linkage in the age of genomics

- Whole genome sequencing is becoming more and more powerful and available
- Is linkage analysis still necessary?



**Table 1 | Summary of 1000 Genomes Project phase I data**

	Autosomes	Chromosome X	GENCODE regions*
Samples	1,092	1,092	1,092
Total raw bases (Gb)	19,049	804	327
Mean mapped depth (×)	5.1	3.9	80.3
SNPs			
No. sites overall	36.7 M	1.3 M	498 K
Novelty rate†	58%	77%	50%
No. synonymous/non-synonymous/nonsense	NA	4.7/6.5/0.097 K	199/293/6.3 K
Average no. SNPs per sample	3.60 M	105 K	24.0 K
Indels			
No. sites overall	1.38 M	59 K	1,867
Novelty rate†	62%	73%	54%
No. inframe/frameshift	NA	19/14	719/1,066
Average no. indels per sample	344 K	13 K	440
Genotyped large deletions			
No. sites overall	13.8 K	432	847
Novelty rate†	54%	54%	50%
Average no. variants per sample	717	26	39

NA, not applicable.

\* Autosomal genes only.

† Compared with dbSNP release 135 (Oct 2011), excluding contribution from phase I 1000 Genomes Project (or equivalent data for large deletions).

\*Lists of participants and their affiliations appear at the end of the paper.

# An integrated map of genetic variation from 1,092 human genomes

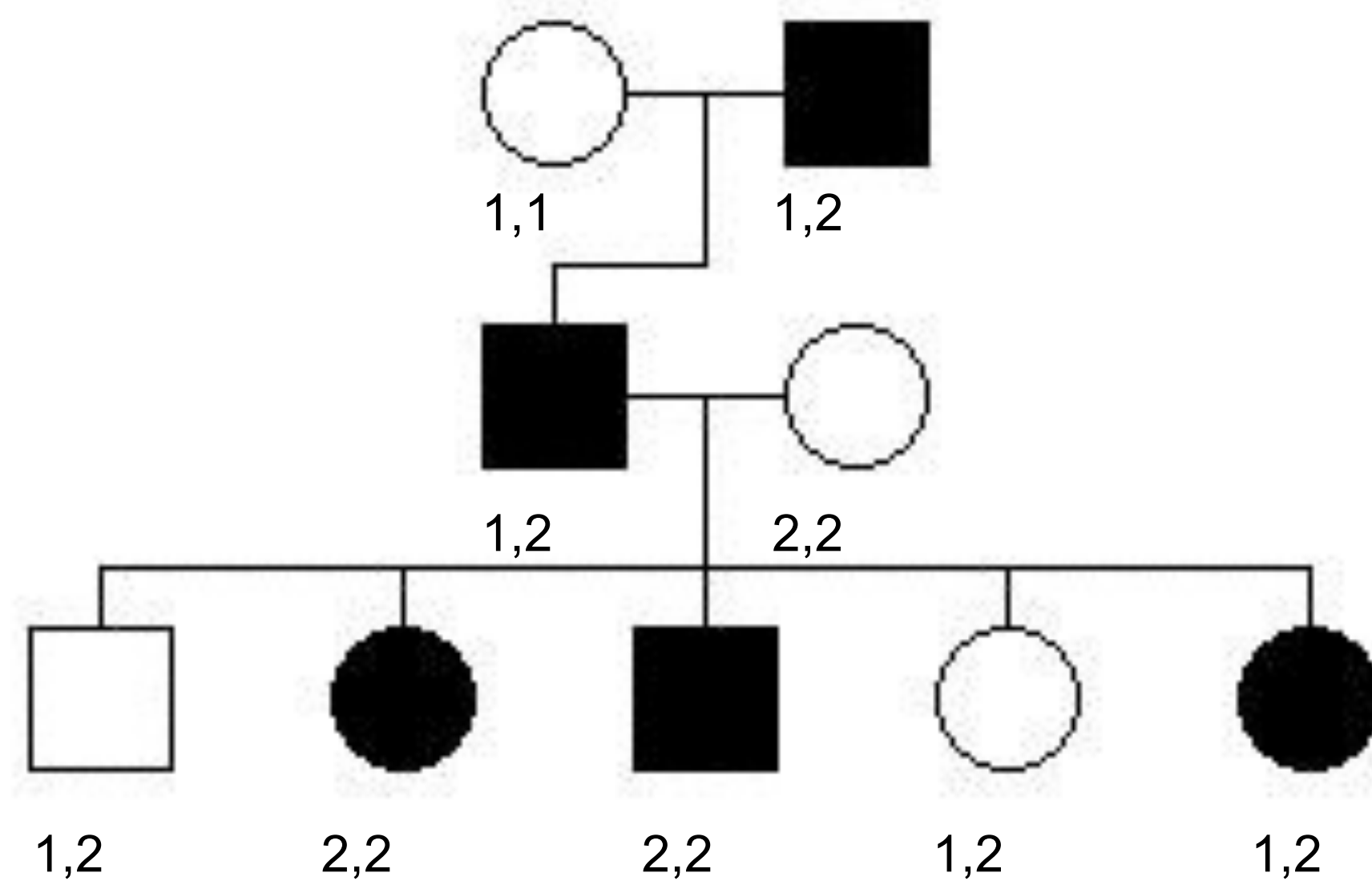
The 1000 Genomes Project Consortium\*



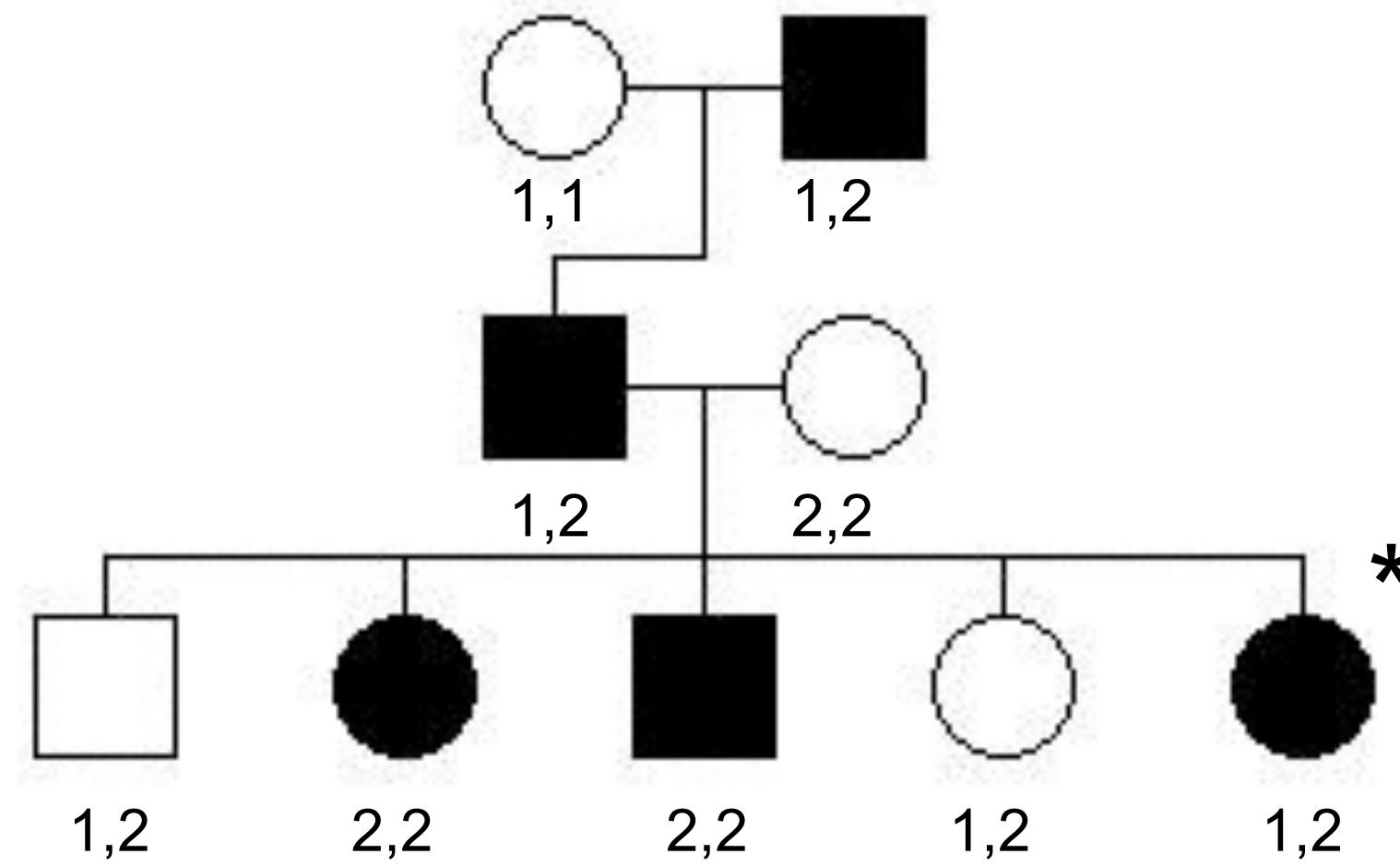
# Linkage in the age of genomics

- We can expect millions of sequence differences between two individuals
  - Less in close relatives, but still a lot
- Which of these differences is responsible for a phenotype is not evident
  - Easier in coding regions
- Whole genome (or exome) sequencing is used for very rare disorders (not enough cases for linkage)







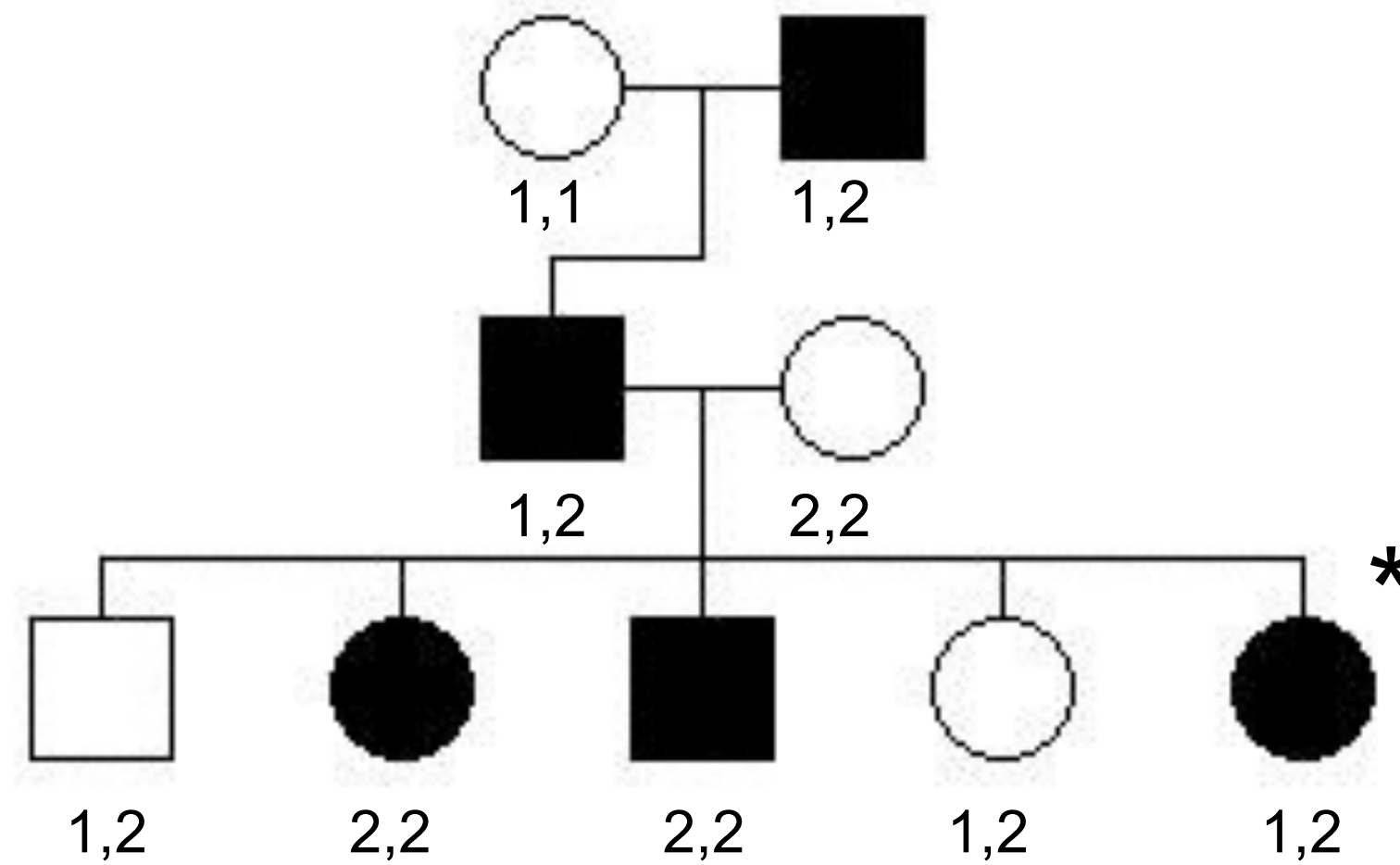


1 recombinant (R); 4 non-recombinant (NR)

Assuming no linkage ( $\theta=0.5$ ) probability of getting either R i NR is the same and equals  $\frac{1}{2}$

$$L(\theta=0,5)= (\frac{1}{2})^5$$





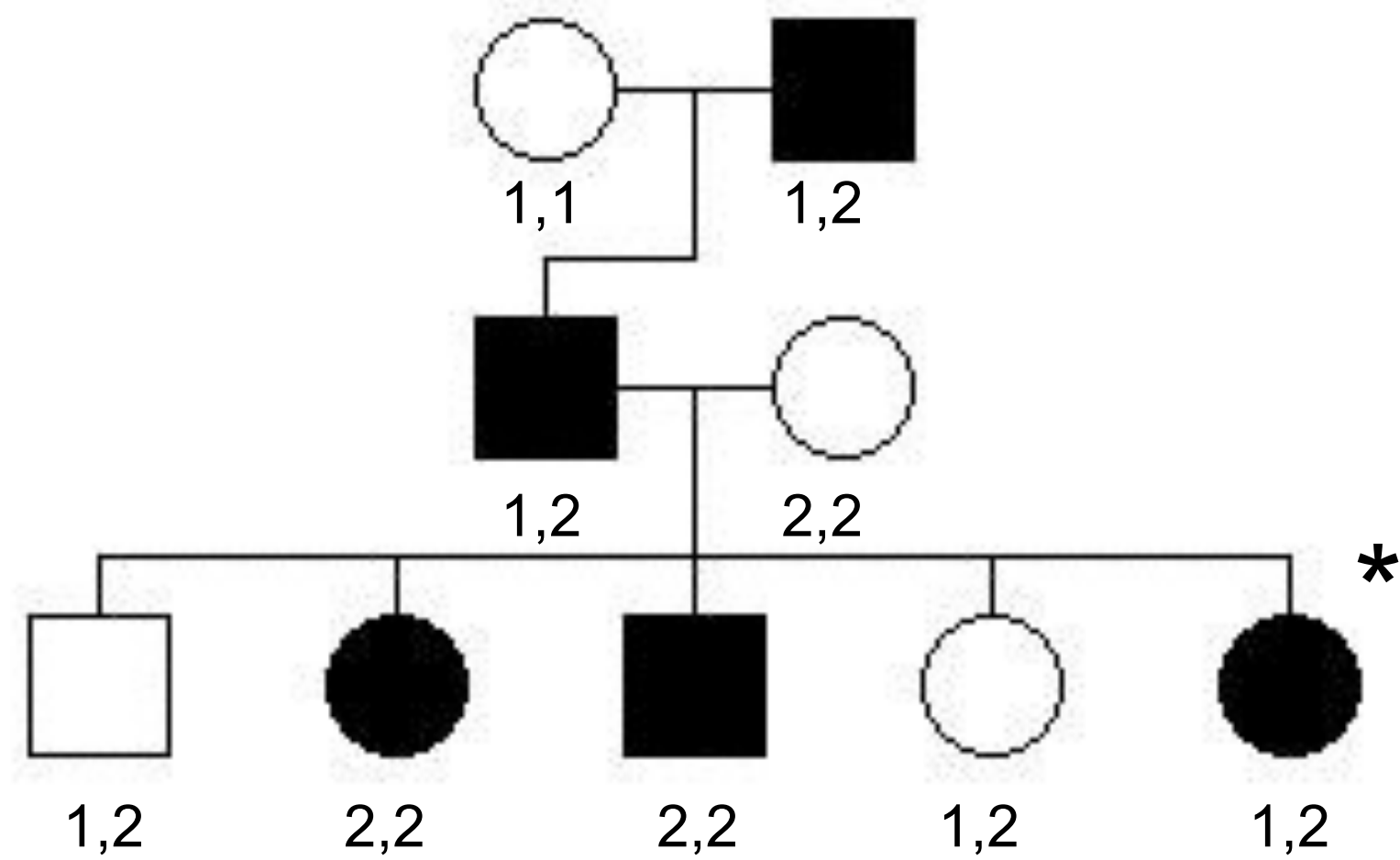
1 recombinant (R); 4 non-recombinant (NR)

For a given  $\theta$  the probability of obtaining R is  $\theta$  (by definition), therefore the probability of obtaining NR is  $1 - \theta$

$$L(\theta) = \theta \cdot (1 - \theta)^4$$

$\nearrow$  1R                       $\nwarrow$  4NR





1 recombinant (R); 4 non-recombinant (NR)

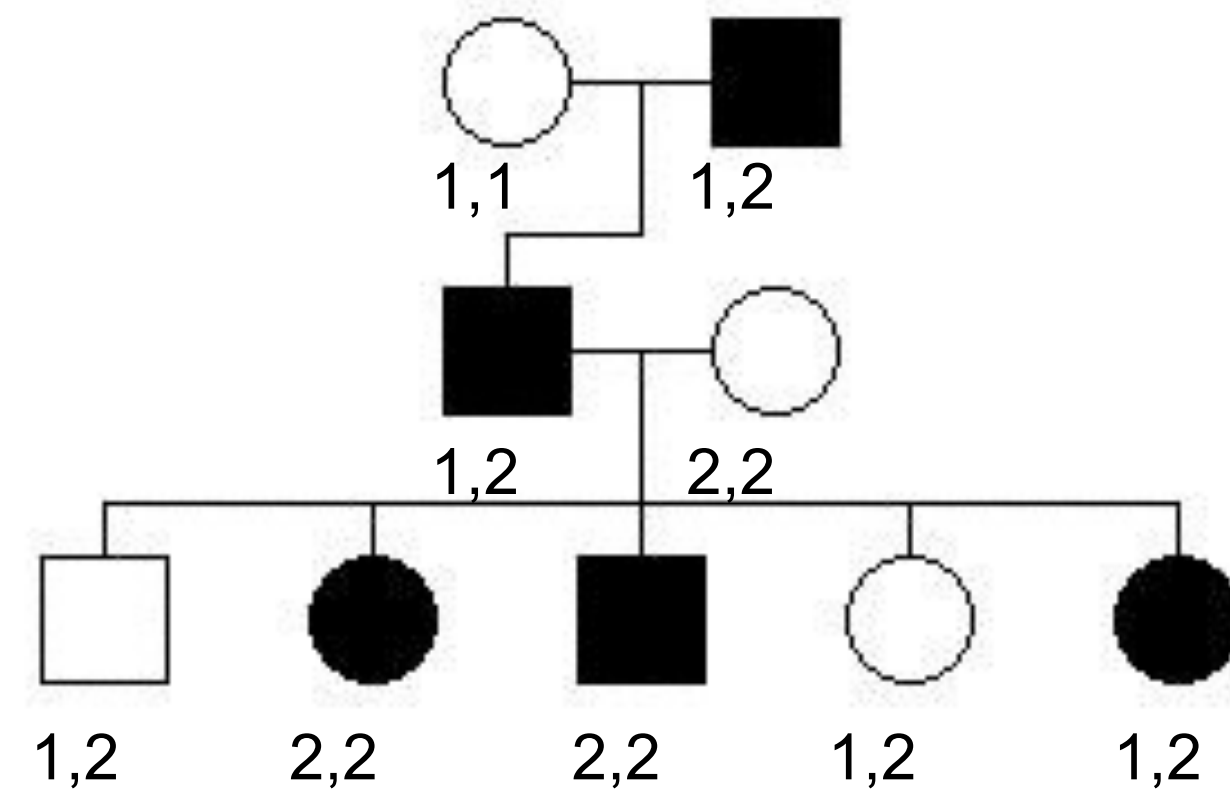
$$L(\theta=0.5) = \left(\frac{1}{2}\right)^5$$

$$L(\theta) = \theta \cdot (1 - \theta)^4$$

$$\text{For } \theta=0.1 \quad L(\theta=0.1) = 0.1 \cdot (0.9)^4$$

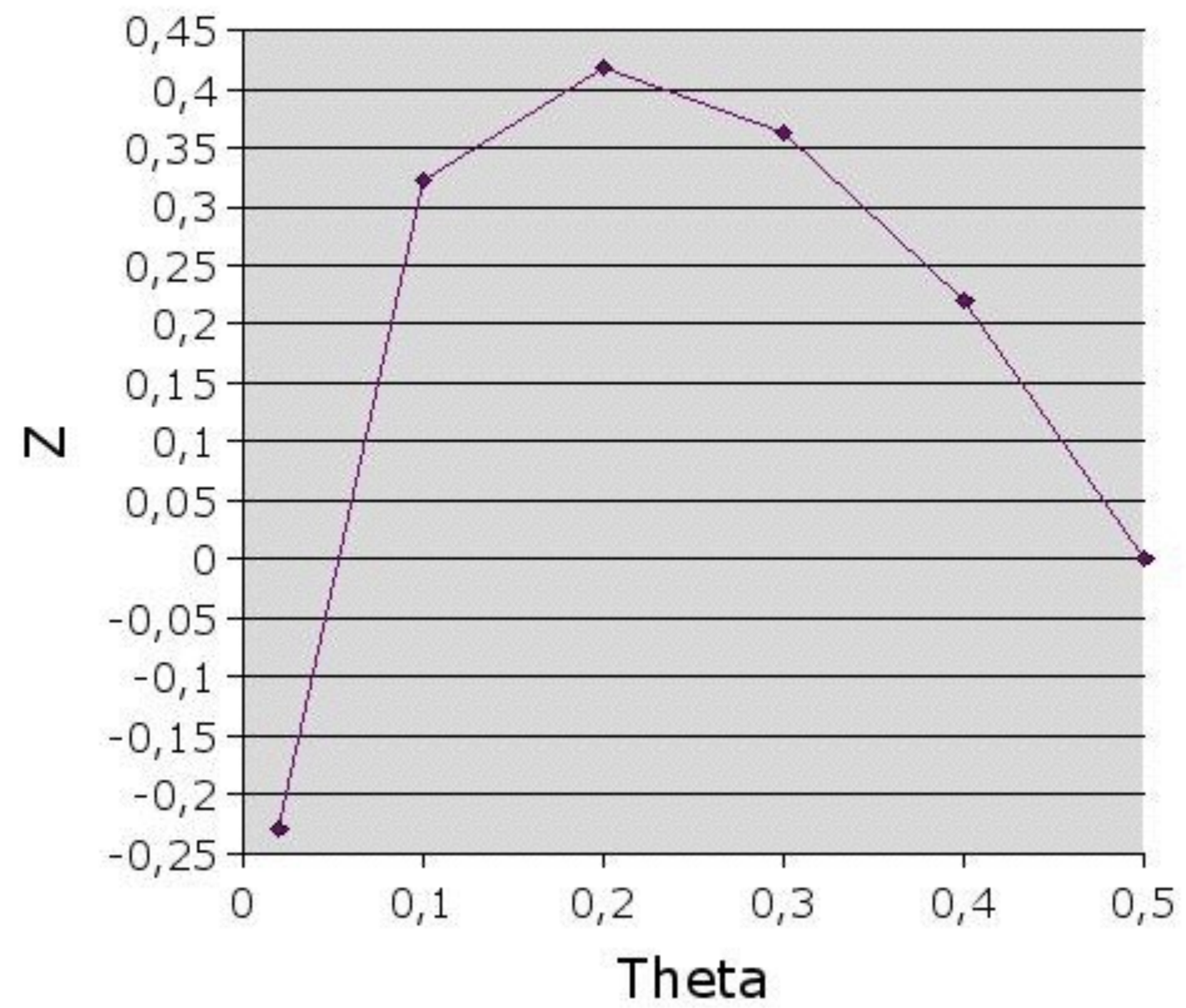
$$Z(\theta = 0,1) = \log_{10} \left( \frac{0,1 \cdot 0,9^4}{0,5^5} \right) \approx 0,32$$





0	0.02	0.1	0.2	0.3	0.4	0.5
$-\infty$	-0.23	0.32	0.42	0.36	0.22	0

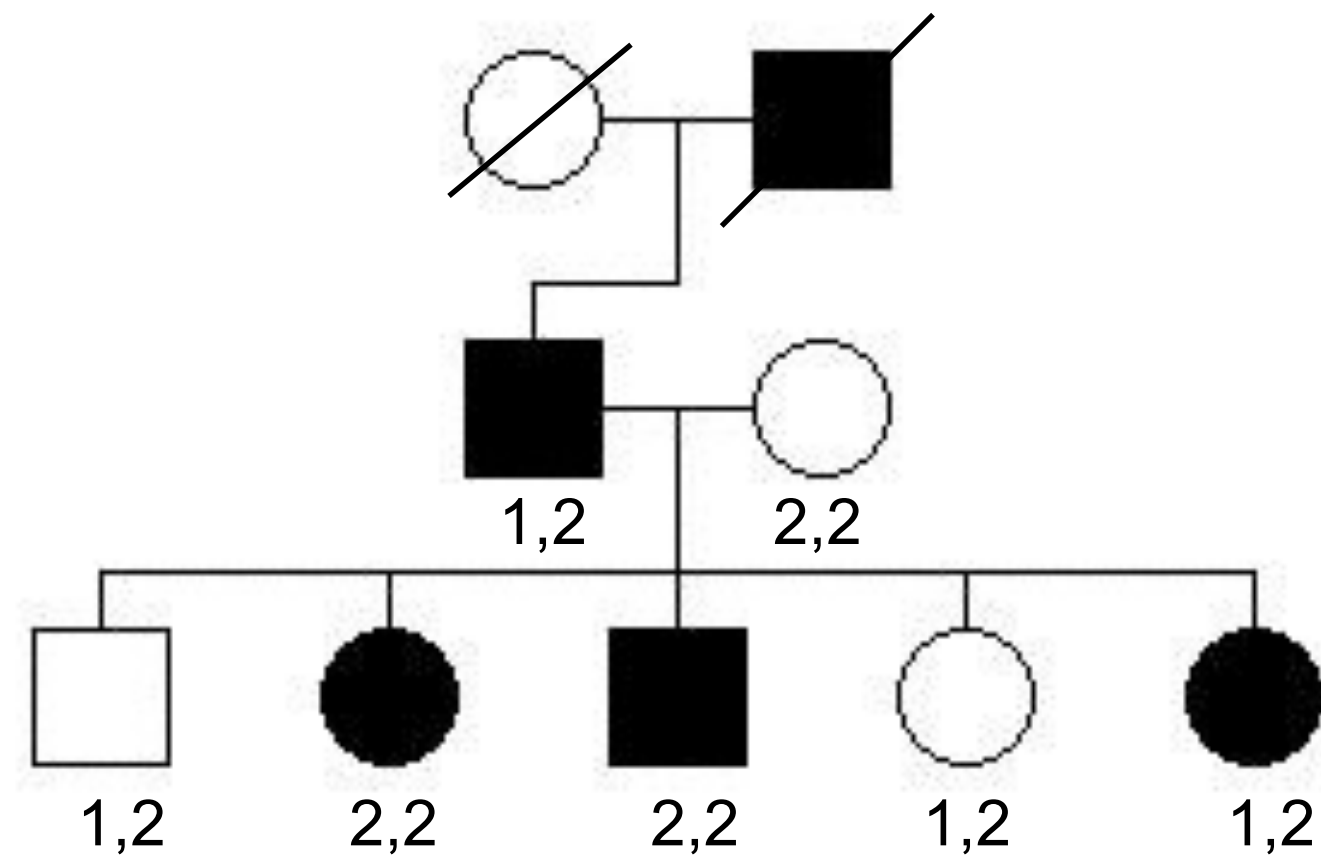




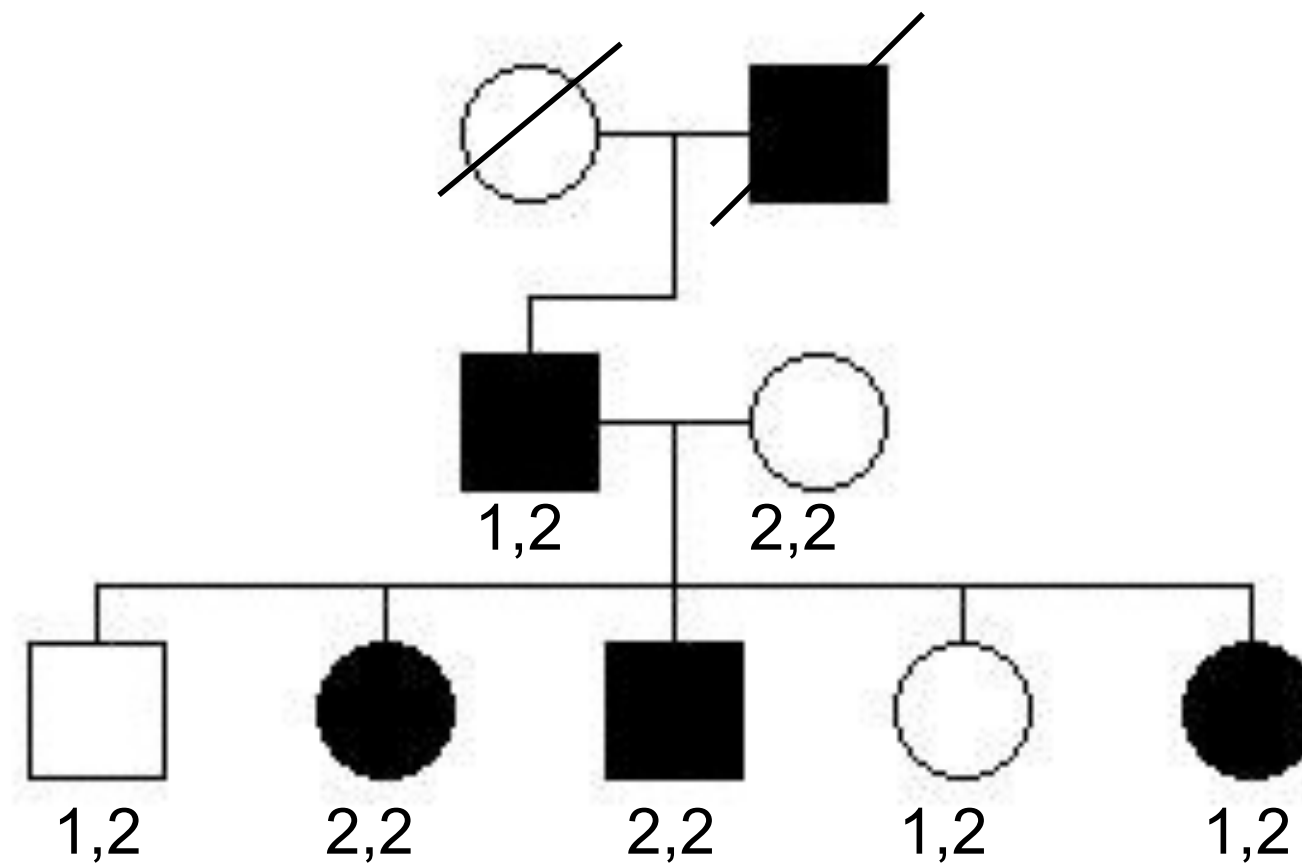
0	0.02	0.1	0.2	0.3	0.4	0.5
$-\infty$	-0.23	0.32	0.42	0.36	0.22	0



# Marker phase in the father unknown







$$\blacksquare \frac{1}{2} +$$

1R 4NR

or

$$\blacksquare \frac{2}{1} +$$

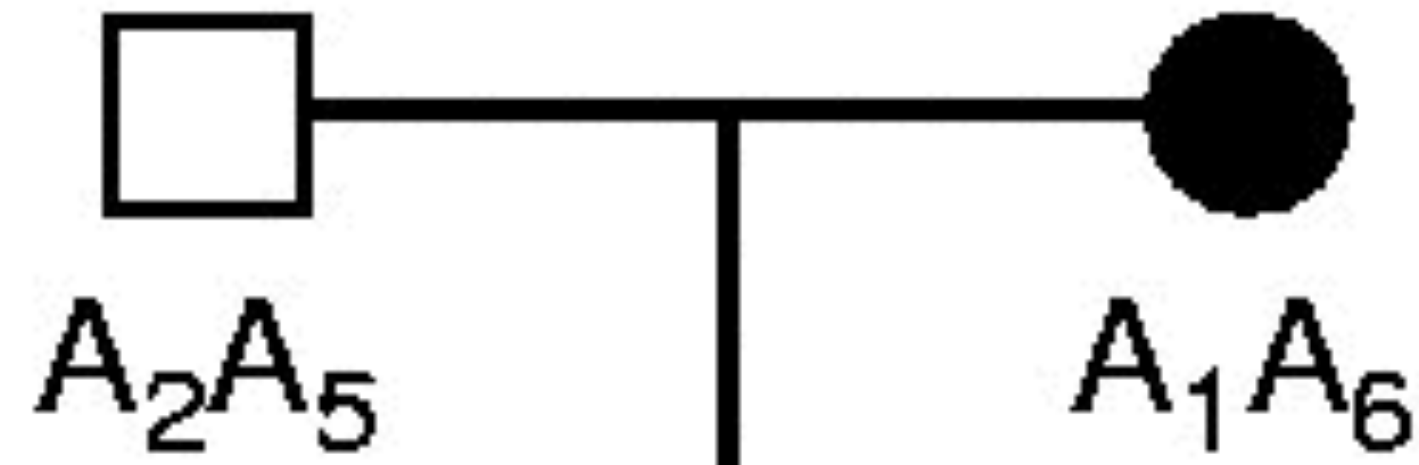
1NR 4R

$$L(\theta = 0,2) = \left( \frac{0,2 \cdot 0,8^4}{2} \right) + L(\theta = 0,2) = \left( \frac{0,2^4 \cdot 0,8}{2} \right)$$

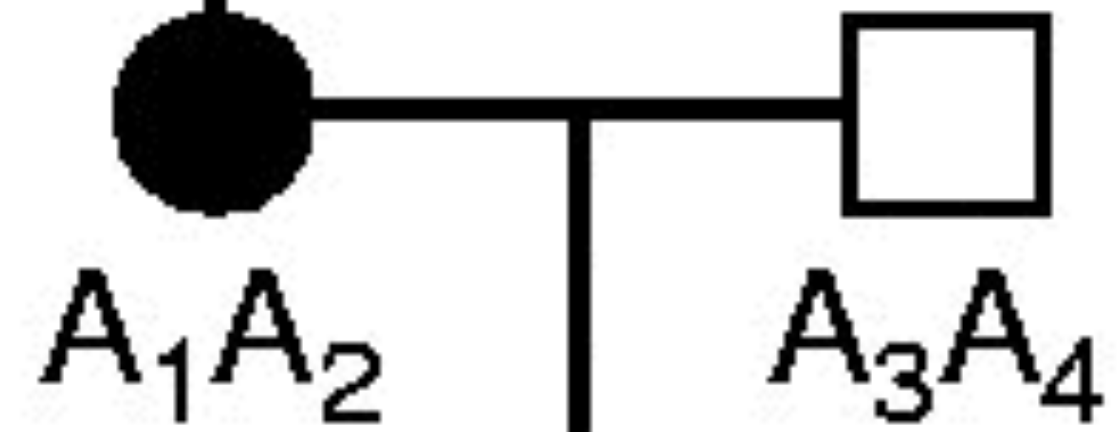
$$Z(\theta = 0,2) = \log_{10} \left( \frac{\frac{0,2 \cdot 0,8^4}{2} + \frac{0,2^4 \cdot 0,8}{2}}{0,5^5} \right) \approx 0,12$$



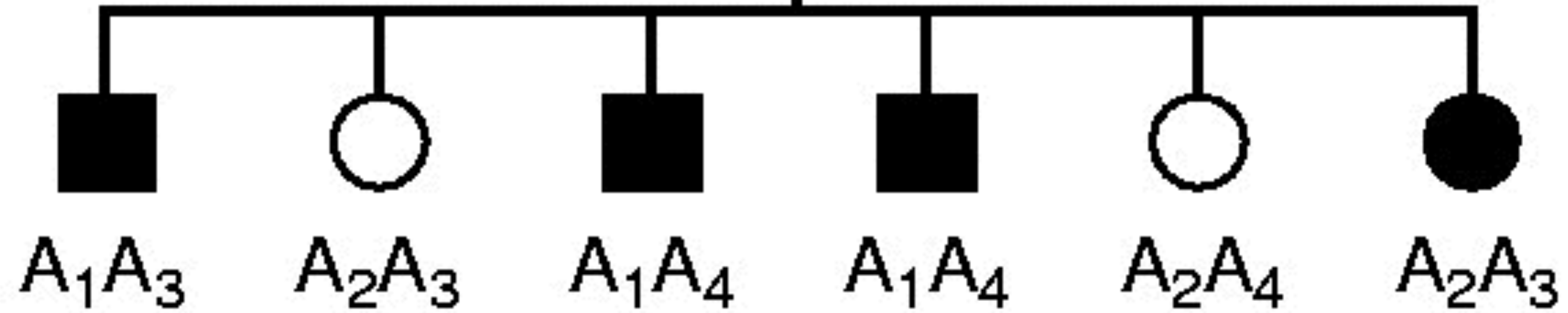
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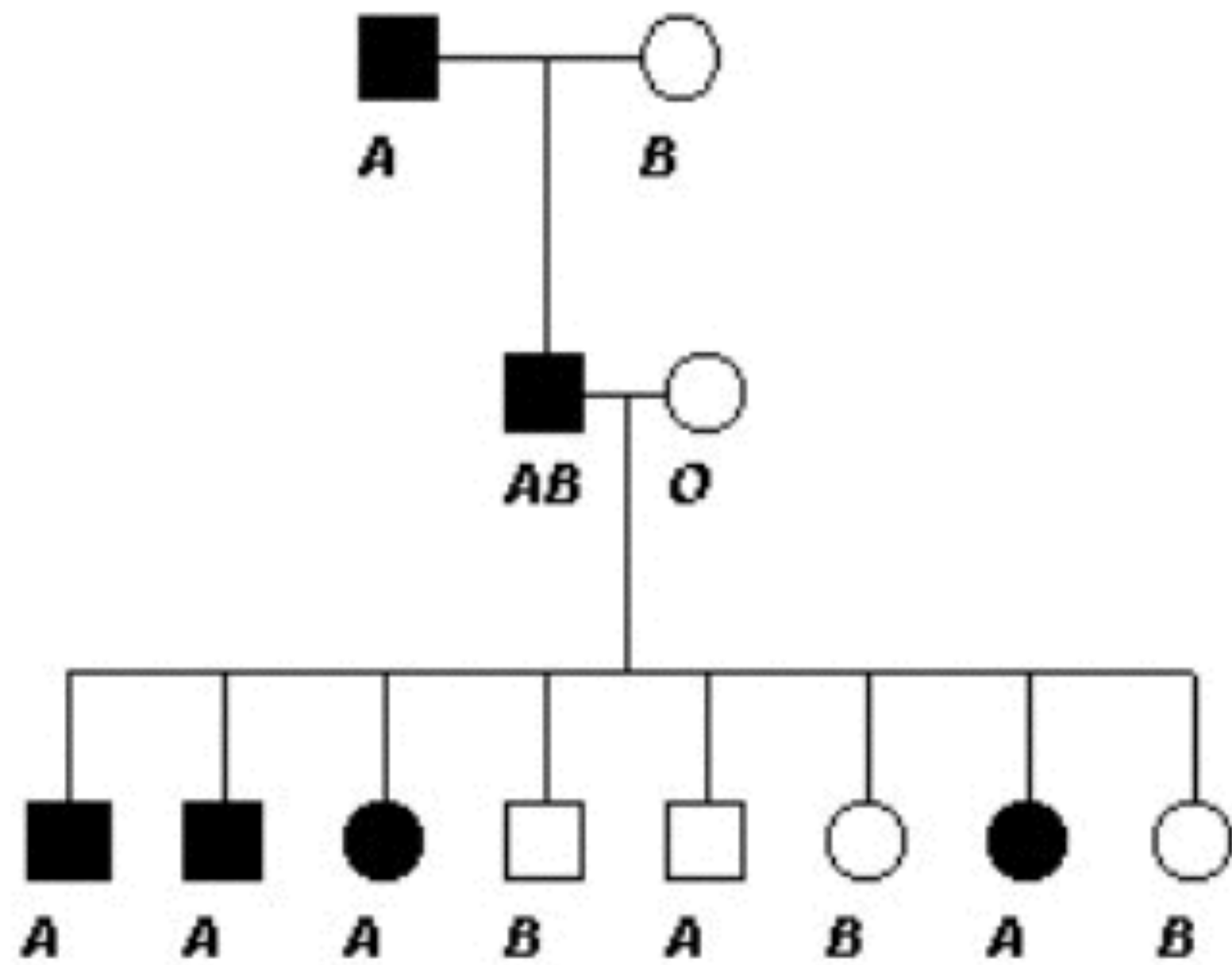
II



III









# Nail-patella syndrome